# Why Lense-Thirring solid-body precession cannot produce the LFQPOs observed in X-ray binaries

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Collaborators: J. Ferreira, P.-O. Petrucci, J. Malzac, C. Reynolds, J. Neilsen, to name a few... This work was in collaboration with J. Neilsen, see Marcel & Neilsen (2021)



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Viscous torque

$$\begin{split} G_{\nu} &= -\left(2\pi R\right)\nu\Sigma R^{2}\frac{\partial\Omega_{\phi}}{\partial R}\\ \text{with }\nu &= \alpha\Omega_{\phi}H^{2} \end{split}$$

Viscous torque  $G_{\nu} = -(2\pi R) \nu \Sigma R^2 \frac{\partial \Omega_{\phi}}{\partial R}$ with  $\nu = \alpha \Omega_{\phi} H^2$  Lense-Thirring torque

 $G_{LT} = (2\pi RH) (\Omega_p L) |\hat{k} \times \hat{I}|$ 



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 $?: \mathbb{A}$ 

Lense-Thirring torque

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$$\frac{G_{LT}}{G_{\nu}} = \frac{4}{3} \frac{a |\sin(\theta)|}{\alpha \epsilon} (R/R_g)^{-3/2}$$

 $\theta$ 







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Wave-like regime ( $\alpha \ll \epsilon$ )

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Bardeen-Petterson configuration

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solid-body precession

The LT precession has shown unprecedented results... but are we in the right conditions?

Frank et al. (2002), Marcel & Neilsen (2021)

$$\dot{M} = 2\pi R | u_R | \Sigma$$
$$\tau = \kappa \Sigma$$
$$\kappa = \sigma_T / m_p$$





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$$\rightarrow$$
 MAD:  $u_R/u_{sound} \gtrsim 1$  (Narayan et al. 2012)

 $\rightarrow$  JED:  $u_R/u_{sound} \approx 1$  by definition (Ferreira et al. 1993a,b, 1995, Marcel et al. 2018a,b)

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Result 2: If the hot flow is turbulent, the expected viscosity is  $\alpha \sim 5$ This is an extreme value... is the hot flow really a 'viscous' flow?

Condition n°1 : 
$$\frac{G_{LT}}{G_{\nu}} = \frac{4}{3} \frac{a |\sin(\theta)|}{\alpha \epsilon} (R/R_g)^{-3/2} > 1$$

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$$\frac{G_{LT}}{G_{\nu}} \simeq 0.04 \times \left(\frac{L_{Edd}/c^2}{\dot{M}}\right) \cdot \left(\frac{\epsilon}{0.2}\right) \cdot \left(\frac{\tau}{1}\right) \cdot \left(\frac{10\,R_g}{R}\right)$$
$$\alpha \simeq 5.3 \times \left(\frac{\dot{M}}{L_{Edd}/c^2}\right) \cdot \left(\frac{0.2}{\epsilon}\right)^2 \cdot \left(\frac{1}{\tau}\right) \cdot \left(\frac{10\,R_g}{R}\right)^{1/2}$$

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Result 3: The conditions for LT solid-body precession are not fulfilled in the luminous hard states...

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3 - The solid-body precession model, in its current form, is inconsistent with both of these conclusions... But there is still hope:

—> Address the impact of the high sound speed and the new torque on the bending waves